

## FULLY WORKED SOLUTIONS

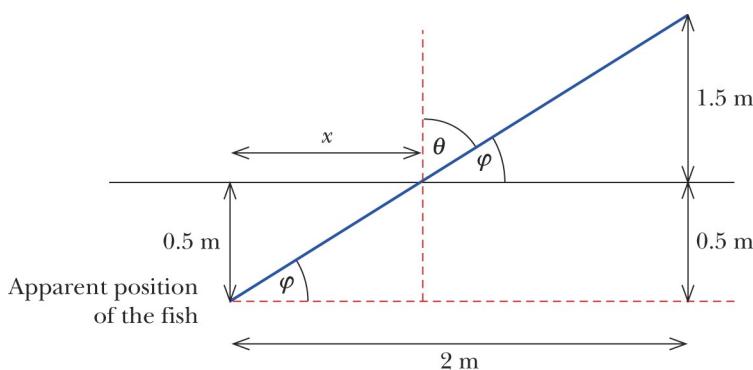
### Chapter 15: Seeing the light

#### Chapter questions

1.  $\lambda = v/f = 30/200 = 0.15 \text{ m}$
2.  $\lambda = 6 \text{ m}, f = 1/3 \text{ Hz}$   
 $v = f\lambda = 6 \times 1/3 = 2 \text{ m s}^{-1}$
3.  $\lambda = 1.3 \text{ m}, v = 330 \text{ m s}^{-1}$   
 $f = v/\lambda = 330/1.3 = 254 \text{ Hz}$
4.  $n_x = 3 \times 10^8 / 2.1 \times 10^8 = 1.43$
5.  $f_{\text{in window glass}} = f_{\text{in air}}$   
 $f = v/\lambda = 3 \times 10^8 / 4.20 \times 10^{-7} = 7.14 \times 10^{14} \text{ Hz}$
6.  $v = c/n_{\text{diamond}} = 3 \times 10^8 / 2.42 = 1.24 \times 10^8 \text{ m s}^{-1}$
7.  $n_w = 1.33, n_g = 1.53, \theta_g = 49^\circ$   
 $\sin \theta_w = n_g \sin \theta_g / n_w = 1.53 \times \sin 49^\circ / 1.33 = 0.87$   
 $\theta_w = 60^\circ$
8.  $\sin \theta_w = n_a \times \sin \theta_a / n_w = 1 \times \sin 15^\circ / 1.33 = 0.195$   
 $\theta_w = 11.2^\circ$
9.  $\theta_a = 60^\circ, n_a = 1, n_g = 1.51$   
 $\sin \theta_g = n_a \sin \theta_a / n_g = 1 \times \sin 60^\circ / 1.51 = 0.574$   
 $\theta_g = 35^\circ$   
 $x = 4 \tan 35^\circ = 2.8 \text{ cm}$

#### Review questions

9.  $v = 4 \text{ m s}^{-1}, f = 10 \text{ s}^{-1}$   
 $\lambda = \frac{v}{f} = \frac{4}{10} = 0.4 \text{ m}$
10. We can construct the following diagram:



Let  $x$  be the horizontal distance of the fish from the normal.

$$\tan \varphi = \frac{2}{2} = 1$$

$$\varphi = 45^\circ$$

$$x = \frac{0.5}{\tan 45^\circ} = 0.5 \text{ m}$$

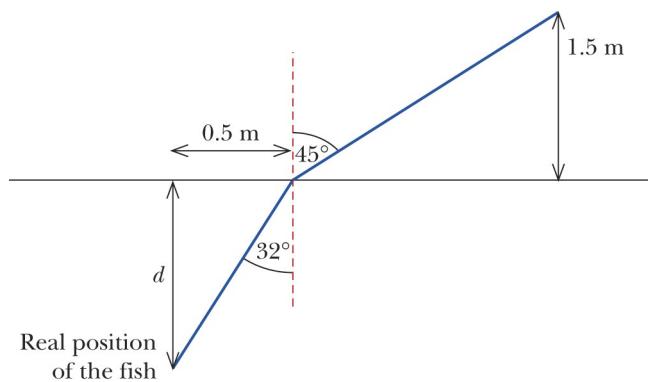
$$\theta_1 = 90^\circ - 45^\circ = 45^\circ$$

$$n_1 = 1, n_2 = 1.33, \theta_1 = 45^\circ$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1 \times \sin 45^\circ = 1.33 \sin \theta_2$$

$$\theta_2 = 32^\circ$$



$$\tan 32^\circ = \frac{0.5}{d}$$

$$d = \frac{0.5}{\tan 32^\circ} = 0.8 \text{ m}$$

Therefore, the fish is located 0.8 m below the surface of the water.

12. (a)  $\theta_1 = 30^\circ, n_1 = 1, n_2 = 1.33$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1 \times \sin 30^\circ = 1.33 \times \sin \theta_2$$

$$\sin \theta_2 = 0.38$$

$$\theta = 22^\circ$$

(b)  $\theta_1 = 40^\circ, n_1 = 1, n_2 = 1.33$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1 \times \sin 40^\circ = 1.33 \times \sin \theta_2$$

$$\theta = 29^\circ$$

Therefore  $\theta_2$  is  $7^\circ$  larger.

13. 1 m

14. HIMOTUVWX

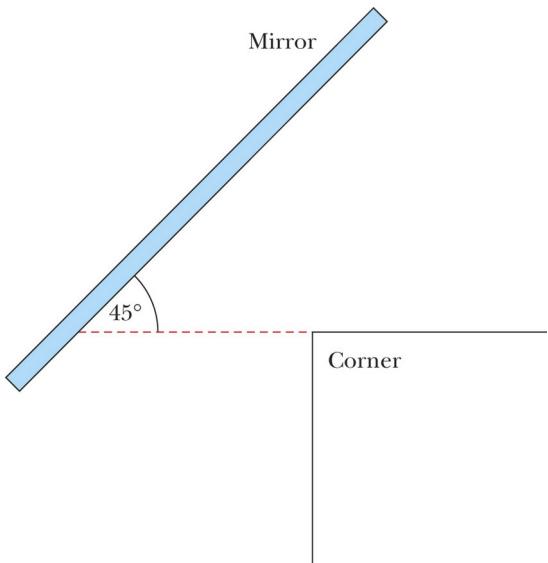
15. (a) Plot  $\sin \theta_1$  on the  $y$ -axis and  $\sin \theta_2$  on the  $x$ -axis. The gradient of the line of best fit will be equal to  $n_2/n_1$  or, in this case,  $n_2$ .

(b)

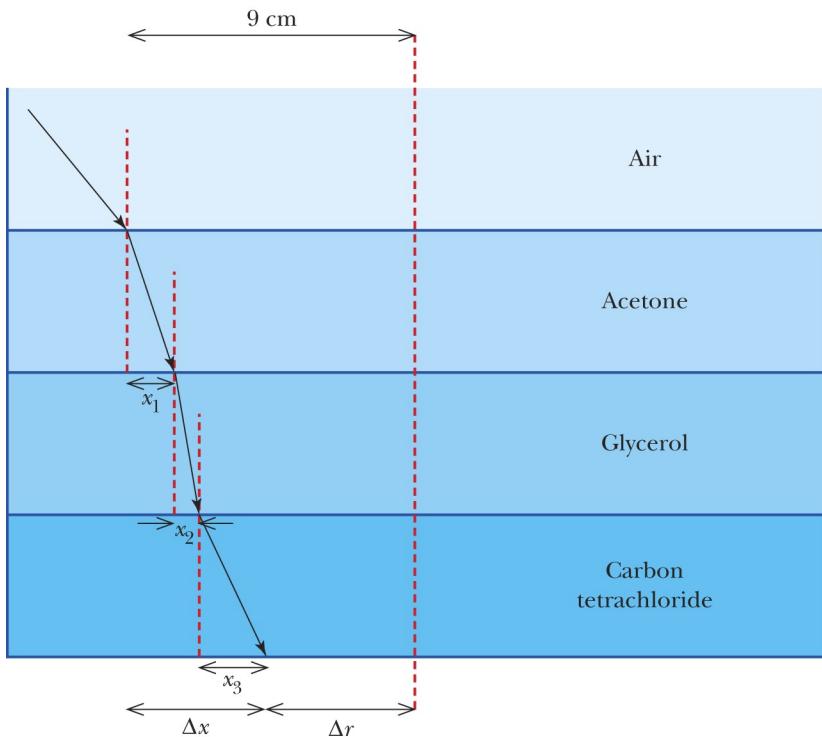
$\theta_1$	$\theta_2$	$\sin \theta_1$	$\sin \theta_2$	$\sin \theta_1/\sin \theta_2$
0	0	0	0	
10	6	0.174	0.105	1.6
20	12	0.342	0.208	1.6
30	18	0.5	0.309	1.6
40	24	0.643	0.407	1.6
50	29	0.766	0.485	1.6
60	33	0.866	0.545	1.6

Therefore  $n_2 = 1.6$ .

16.



17.



In going from air to the acetone layer:

$$n_{\text{air}} \sin \theta_{\text{air}} = n_{\text{acetone}} \sin \theta_{\text{acetone}}$$

$$1 \times \sin 25^\circ = 1.357 \times \sin \theta_{\text{acetone}}$$

$$\sin \theta_{\text{acetone}} = 0.311$$

$$\theta_{\text{acetone}} = 18.14^\circ$$

$$x_1 = 1.5 \times \tan 18.14^\circ = 0.492 \text{ cm}$$

In going from the acetone layer to the glycerol layer:

$$n_{\text{acetone}} \sin \theta_{\text{acetone}} = n_{\text{glycerol}} \sin \theta_{\text{glycerol}}$$

$$1.357 \times \sin 18.14^\circ = 1.474 \times \sin \theta_{\text{glycerol}}$$

$$\theta_{\text{glycerol}} = 16.6^\circ$$

$$x_2 = 1.5 \times \tan 16.6^\circ = 0.449 \text{ cm}$$

In going from the glycerol layer to the carbon tetrachloride layer:

$$n_{\text{glycerol}} \sin \theta_{\text{glycerol}} = n_{\text{carbon tetrachloride}} \sin \theta_{\text{carbon tetrachloride}}$$

$$1.4746 \times \sin 16.6^\circ = 1.4601 \times \sin \theta_{\text{carbon tetrachloride}}$$

$$\theta_{\text{carbon tetrachloride}} = 16.8^\circ$$

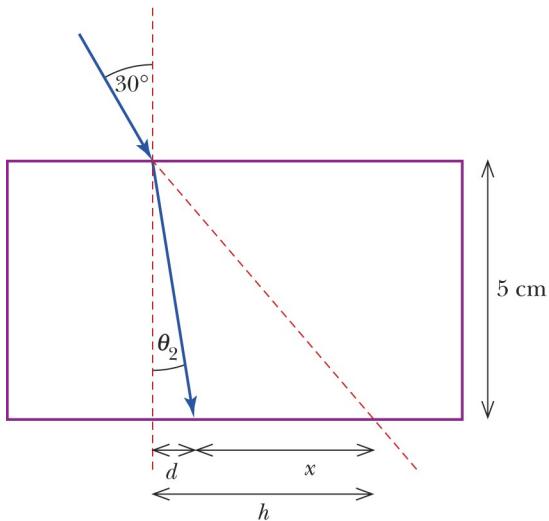
$$x_3 = 1.5 \times \tan 16.8^\circ = 0.452 \text{ cm}$$

$$\Delta x = x_1 + x_2 + x_3 = 0.492 + 0.449 + 0.452 = 1.4 \text{ cm}$$

$$\Delta r = 9 \text{ cm} - 1.4 \text{ cm} = 7.6 \text{ cm}.$$

The ray emerges 7.6 cm from the centre of the beaker.

18.



$$\tan 30^\circ = \frac{h}{5}$$

$$h = 5 \tan 30^\circ = 2.88 \text{ cm}$$

To determine refracted angle:

$$1 \sin 30^\circ = 1.42 \sin \theta_2$$

$$\theta_2 = 20.6^\circ$$

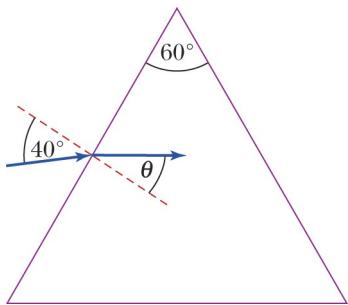
We can see in the diagram above that:

$$\tan 20.6^\circ = \frac{d}{5}$$

$$d = 5 \tan 20.6^\circ = 1.88 \text{ cm}$$

$$x = h - d = 2.88 - 1.88 = 1 \text{ cm}$$

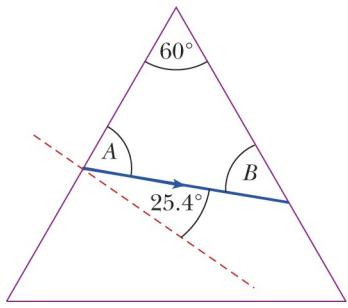
19.



$$n_{\text{air}} \sin 40^\circ = n_{\text{glass}} \sin \theta$$

$$1 \sin 40^\circ = 1.50 \sin \theta$$

$$\theta = 25.4^\circ$$

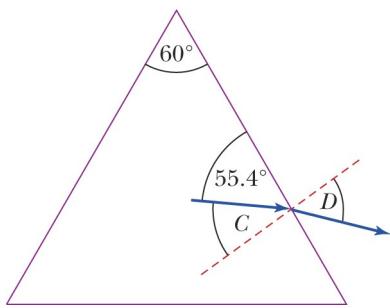


As  $A + 25.4^\circ = 90^\circ$ , then  $A = 64.6^\circ$

Also, as  $60^\circ + A + B = 180^\circ$ ,

$$60^\circ + 64.6^\circ + B = 180^\circ$$

$$\text{so } B = 55.4^\circ$$



$$C + 55.4^\circ = 90^\circ, \text{ so } C = 34.5^\circ$$

$$n_{\text{glass}} \sin C = n_{\text{air}} \sin D$$

$$1.50 \sin 34.5^\circ = 1 \sin D$$

$$0.85 = \sin D^\circ$$

$$D = 58.2^\circ$$